

## THE RESOLVENT OPERATOR OF SINGULAR IMPULSIVE DYNAMIC DIRAC EQUATIONS

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ABSTRACT. In this study, impulsive singular dynamic Dirac equations are considered. Firstly, a spectral function for these equations is constructed. Later, an integral representation of the resolvent operator is obtained.

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